

Recent progress in Higher Spin Gravity and $3d$ bosonization duality

IFS seminar

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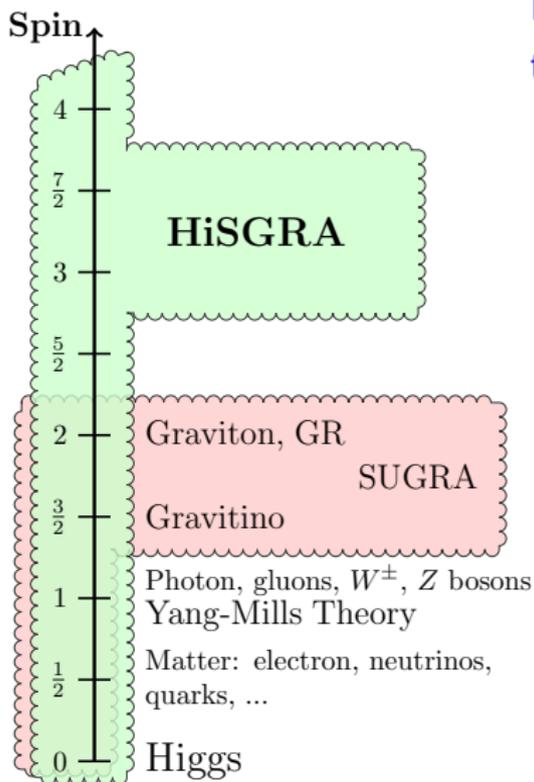
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Main Messages

- Higher spin states, $s > 2$, should be important for Quantum Gravity. UV=massless. Can we have higher spin gravities? **yes, but very few and they are very peculiar**
- There is a class of HiSGRA — **Chiral** — in $4d$ that can be thought of as a higher spin extension of SDYM and SDGR. It has some stringy features and is UV-finite at least at one loop
- **Chiral HiSGRA** is related to (Chern-Simons) vector models and is instrumental in attacking the $3d$ bosonization duality
- **Higher spin symmetry can be interesting on its own**, as an extended conformal symmetry (new Virasoro) and allows us to make general statements about $3d$ bosonization duality
- **plan**: tour over HiSGRA's, applications to $3d$ bosonization and higher spin symmetries

Why higher spins?



Different spins lead to very different types of theories/physics:

- $s = 0$: Higgs
- $s = 1/2$: Matter

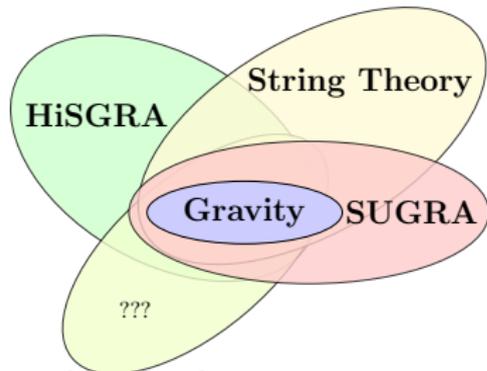
- $s = 1$: Yang-Mills, Lie algebras
- $s = 3/2$: SUGRA and supergeometry, graviton \in spectrum
- $s = 2$ (graviton): GR and Riemann Geometry, no color

- $s > 2$: HiSGRA and String theory, ∞ states, graviton is there too!

Why higher spin particles?

Various examples

- string theory
- divergences in (SU)GRA's
- Quantum Gravity via AdS/CFT



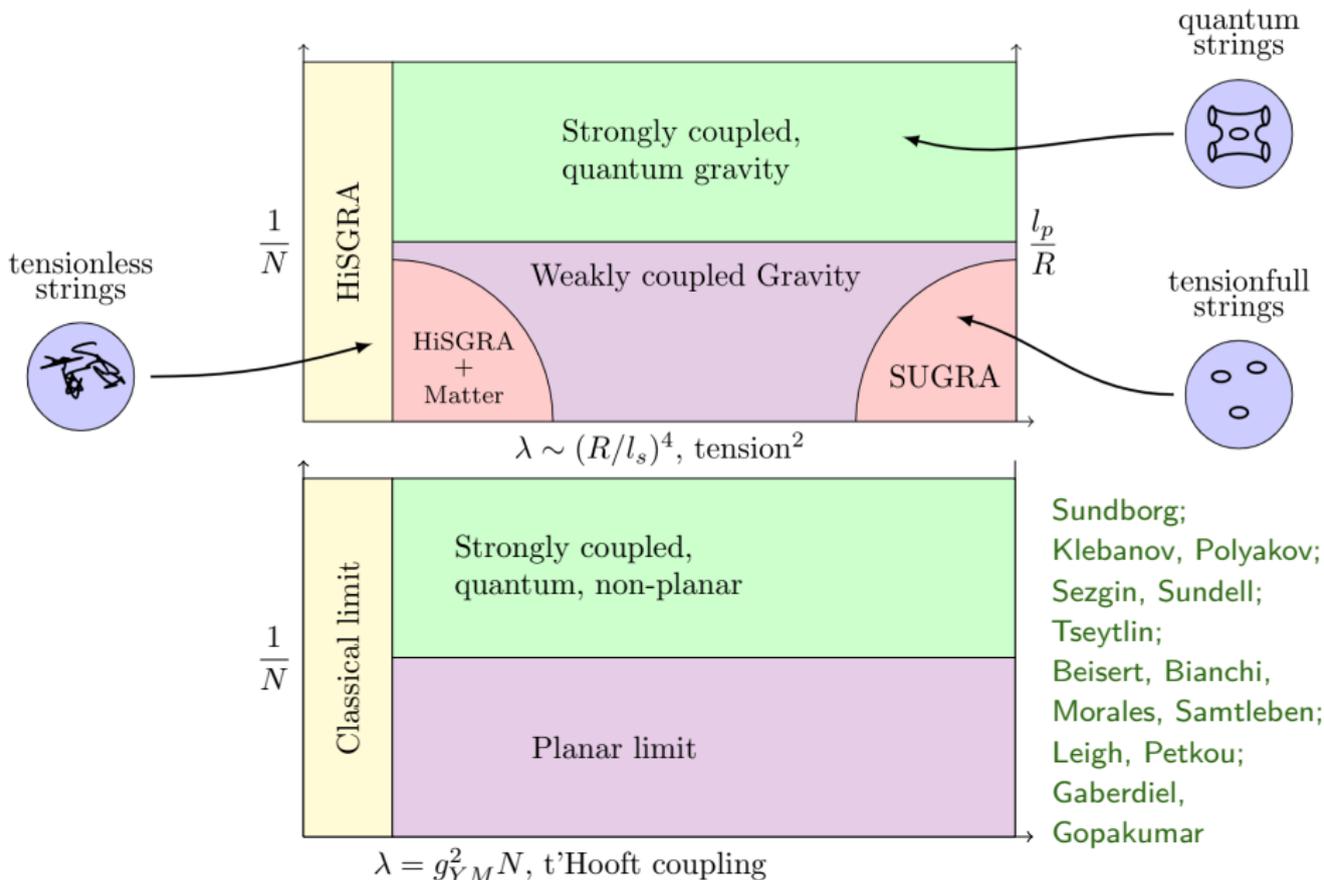
seem to indicate that quantization of gravity requires

- infinitely many states (can take massless in UV regime?)
- the spectrum is unbounded in spin

HiSGRA is to find the most minimalistic extension of gravity by massless, i.e. gauge, higher spin fields. Vast gauge symmetry should render it finite.

Quantizing Gravity via HiSGRA \approx Constructing Classical HiSGRA

HiSGRA from Tensionless Strings, duals of weakly coupled CFT's



Why massless higher spins should not exist?

	Flat	(A)dS
Global		
Local		

Why massless higher spins should not exist?

	Flat	(A)dS
Global	<p>decoupling of longitudinal modes $\delta\Phi_{a_1\dots a_s} = \partial_{(a_1}\xi_{a_2\dots a_s)}$, or tensorial charges $Q_{a_1\dots a_{s-1}}$</p> <p>impose ∞-many constraints: $S = \mathbf{1}^{**}$</p> <p>(Weinberg; Coleman, Mandula)</p>	
Local		

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Constraints on (holographic) S-matrix

Asymptotic higher spin symmetries (HSS)

$$\delta\Phi_{\mu_1\dots\mu_s}(x) = \nabla_{(\mu_1}\xi_{\mu_2\dots\mu_s)}$$

seem to completely fix (holographic) S-matrix to be

$$S_{\text{HiSGRA}} = \begin{cases} 1^{***}, & \text{flat space,} \\ \text{free CFT,} & \text{AdS, unbroken HSS,} \end{cases} \left(\begin{array}{l} \text{Sundborg; Klebanov, Polyakov; Sezgin,} \\ \text{Sundell; Leigh, Petkou; Maldacena,} \\ \text{Zhiboedov; Giombi, Yin, ...} \end{array} \right)$$

Chern-Simons Matter, AdS₄, slightly-broken HSS

Trivial/known S-matrix can still be helpful for QG toy-models

The most interesting applications are to three-dimensional dualities (power of HSS is underexplored)

Both Minkowski and AdS cases reveal certain non-localities to be tamed. HSS mixes ∞ spins and derivatives, invalidating the local QFT approach

Four classes of local HiSGRA in 2022

3d massless and partially-massless (Blencowe, Bergshoeff, Stelle, Campoleoni, Fredenhagen, Pfenninger, Theisen, Henneaux, Rey, Gaberdiel, Gopakumar, Grumiller, Grigoriev, Mkrtchyan, E.S., ...), $S = S_{CS}$ for a higher spin extension of $sl_2 \oplus sl_2$

$$S_{CS} = \int \omega d\omega + \frac{2}{3}\omega^3$$

3d conformal (Pope, Townsend; Fradkin, Linetsky; Grigoriev, Lovrekovic, E.S.), $S = S_{CS}$ for higher spin extension of $so(3, 2)$

4d conformal (Tseytlin, Segal; Bekaert, Joung, Mourad; McLoughlin, Adamo, Tseytlin), higher spin extension of Weyl gravity, local Weyl symmetry tames non-localities

$$S = \int \sqrt{g} (C_{\mu\nu, \lambda\rho})^2 + \dots \quad S \log \Lambda \in \text{Eff.Action}$$

4d massless chiral (Metsaev; Ponomarev, E.S.; Ponomarev; E.S., Tran, Tsulaia; E.S.). The (only) smallest higher spin theory with propagating fields. **This talk!**

The theories avoid all no-go's. Surprisingly, all of them have simple actions and are clearly well-defined, as close to Field Theory as possible

Other ideas and proposals

- **Reconstruction:** invert AdS/CFT
 - Brute force (Bekaert, Erdmenger, Ponomarev, Sleight; Taronna, Sleight)
 - Collective Dipole (Jevicki, Mello Koch et al; Aharony et al)
 - Holographic RG (Leigh et al, Polchinski et al)
- **IKKT matrix model for fuzzy H_4** (Steinacker, Sperling, Fredenhagen, Tran)
- **Formal HiSGRA:** constructing L_∞ -extension of HS algebras, i.e. a certain odd Q , $QQ = 0$, and write AKSZ sigma model (Barnich, Grigoriev)

$$dW = Q(W)$$

Warning: Boulanger,
Kessel, E.S., Taronna

(Vasiliev; E.S., Sharapov, Bekaert, Grigoriev, Tran, Bonezzi, Boulanger, Sezgin, Sundell, Neiman) AdS/CFT: (Sezgin, Sundell, Klebanov, Polyakov, Giombi, Yin, ...)
Complete local theory: Chiral HiSGRA (E.S., Sukhanov, Sharapov, Van Dongen)

Certain things do work, but the general rules are yet to be understood, e.g. non-locality, relation to field theory, quantization, ...

What Higher Spin Problem is: Field theory approach

A massless spin- s particle can be described by a rank- s tensor

$$\delta\Phi_{\mu_1\dots\mu_s} = \nabla_{\mu_1}\xi_{\mu_2\dots\mu_s} + \text{permutations}$$

which generalizes $\delta A_\mu = \partial_\mu\xi$, $\delta g_{\mu\nu} = \nabla_\mu\xi_\nu + \nabla_\nu\xi_\mu$

Fronsdal, Berends, Burgers, Van Dam, Bengtsson², Brink, Metsaev, ..., Bekaert, Boulanger, Sundell, Manvelyan, Mkrtchyan, Francia, Taronna, Joung, ... many many (almost everyone in HS)

Problem: find a nonlinear completion (action, gauge symmetries)

$$S = \int (\nabla\Phi)^2 + \mathcal{O}(\Phi^3) + \dots \quad \delta\Phi\dots = \nabla.\xi\dots + \dots$$

and prove that it is UV-finite, hence a Quantum Gravity model

Warning: brute force does not seem to work!

a bit of concrete higher spins

Three-dimensional HiSGRA

Three-dimensional HiSGRA

The problem is the same: too many structures one can write with $\Phi_{\mu_1 \dots \mu_s}$ and ∂_μ , but much better understanding of cubic and higher vertices (Fredenhagen, Krüger Mkrtychyan; Kessel, Mkrtychyan; Mkrtychyan).

It is easy to show that the problem is equivalent to $QQ = 0$ with Q

$$Q = AA \frac{\partial}{\partial A} \qquad A = \oplus A_\mu^{a_1 \dots a_k} dx^\mu$$

Therefore (Grigoriev, Mkrtychyan, E.S), all such theories are Chern-Simons:

$$S = \text{Tr} \int AdA + \frac{2}{3} A^3$$

where A is a connection of some Lie algebra $\ni sl_2$.

In particular, it is possible to construct first examples with partially-massless fields and many conformal HiSGRA (Grigoriev, Lovrekovic, E.S.)

a bit of concrete higher spins

Chiral Higher Spin Gravity

Self-dual Yang-Mills in Lorentzian signature is a useful analogy

- the theory is non-unitary due to the interactions ($A_\mu \rightarrow \Phi^\pm$)

$$\mathcal{L}_{\text{YM}} = \text{tr } F_{\mu\nu} F^{\mu\nu}$$

\rightsquigarrow

$$\mathcal{L}_{\text{SDYM}} = \Phi^- \square \Phi^+ + V^{++-} + V^{--+} + V^{+-}$$

- tree-level amplitudes vanish, $A_{\text{tree}} = 0$
- one-loop amplitudes do not vanish, are rational and coincide with $(++\dots+)$ of pure QCD
- Yang-Mills Theory as a perturbation of SDYM is a fruitful idea
- integrability, instantons, ...

Chiral HiSGRA (Metsaev; Ponomarev, E.S.) is a 'higher spin extension' of SDYM/SDGR. It has fields of all spins $s = 0, 1, 2, 3, \dots$:

$$\mathcal{L} = \sum_{\lambda} \Phi^{-\lambda} \square \Phi^{+\lambda} + \sum_{\lambda_i} \frac{\kappa l_{\text{Pl}}^{\lambda_1 + \lambda_2 + \lambda_3 - 1}}{\Gamma(\lambda_1 + \lambda_2 + \lambda_3)} V^{\lambda_1, \lambda_2, \lambda_3}$$

light-cone gauge is very close to the spinor-helicity language

$$V^{\lambda_1, \lambda_2, \lambda_3} \sim [\mathbf{12}]^{\lambda_1 + \lambda_2 - \lambda_3} [\mathbf{23}]^{\lambda_2 + \lambda_3 - \lambda_1} [\mathbf{13}]^{\lambda_1 + \lambda_3 - \lambda_2}$$

Locality + Lorentz invariance + genuine higher spin interaction result in a unique completion

This is the smallest higher spin theory and it is unique.
Graviton and scalar field belong to the same multiplet

No UV Divergences! One-loop finiteness

Tree amplitudes vanish. The interactions are naively non-renormalizable, the higher the spin the more derivatives:

$$V^{\lambda_1, \lambda_2, \lambda_3} \sim \partial^{|\lambda_1 + \lambda_2 + \lambda_3|} \Phi^3$$

but there are **no UV divergences!** (E.S., Tsulaia, Tran). Some loop momenta eventually factor out, just as in $\mathcal{N} = 4$ SYM, but ∞ -many times.

At one loop we find three factors: (1) SDYM or all-plus 1-loop QCD; (2) higher spin dressing to account for λ_i ; (3) total number of d.o.f.:

$$A_{\text{Chiral}}^{1\text{-loop}} = A_{\text{QCD}, 1\text{-loop}}^{++\dots+} \times D_{\lambda_1, \dots, \lambda_n}^{\text{HSG}} \times \sum_{\lambda} 1$$

d.o.f. = $\sum_{\lambda} 1 = 1 + 2 \sum_{\lambda > 0} 1 = 1 + 2\zeta(0) = 0$ to comply with no-go's, (Beccaria, Tseytlin) and agrees with many results in AdS , where $\neq 0$

Chiral HSGRA in Minkowski

- **stringy 1**: the spectrum is infinite $s = 0, (1), 2, (3), 4, \dots$
- **stringy 2**: admit Chan-Paton factors, $U(N)$, $O(N)$ and $USp(N)$
- **stringy 3**: we have to deal with spin sums \sum_s (worldsheet takes care of this in string theory) and ζ -function helps
- **stringy 4**: the action contains parts of YM and Gravity
- **stringy 5**: higher spin fields soften amplitudes
- consistent with Weinberg etc. $S = 1^{***}$ (in Minkowski)
- gives all-plus QCD or SDYM amplitudes from a gravity

Apart from Minkowski space the theory exists also in (anti)-de Sitter space, where holographic S-matrix turns out to be nontrivial ... and related to Chern-Simons matter theories

Chiral Higher Spin Gravity: covariantization

Each μ equals AA' where $A, B, \dots = 1, 2$ and $A', B', \dots = 1, 2$

$$\sigma_{\mu}^{AA'} v^{\mu} = v^{AA'} \quad v = \begin{pmatrix} t+x & y+iz \\ y-iz & t-x \end{pmatrix}$$

In general we have $V^{A(n), A'(m)}$ and all indices are symmetric. The only anti-symmetric object is invariant $\epsilon_{AB} = -\epsilon_{BA}$, idem. for $\epsilon_{A'B'}$. Abstract Penrose notation:

$$\text{Maxwell :} \quad F_{\mu\nu} = F_{AB}\epsilon_{A'B'} + \epsilon_{AB}F_{A'B'}$$

$$\text{Weyl :} \quad C_{\mu\nu, \lambda\rho} = C_{ABCD}\epsilon_{A'B'}\epsilon_{C'D'} + \epsilon_{AB}\epsilon_{CD}C_{A'B'C'D'}$$

$$\text{Traceless :} \quad \Phi_{\mu(s)} = \Phi_{A(s), A'(s)}$$

Any of $V^{A(n), A'(m)}$ with $n + m = 2s$ can describe a spin- s field. For $n = m = s$ we have a symmetric/Hermitian description. For $m = 2s$, $n = 2s$ we have (conjugate) Weyl tensors $\Psi^{A(2s)}$, $\Psi^{A'(2s)}$.

Self-dual Yang-Mills

With $F_{\mu\nu}^2 = F_{AB}^2 + F_{A'B'}^2$ and with $F \wedge F = F_{AB}^2 - F_{A'B'}^2$, being topological we can massage YM action

$$S_{YM} = \frac{1}{g^2} \int F_{\mu\nu}^2 \sim \frac{1}{g^2} \int F_{AB}^2 \sim \int \Psi^{AB} F_{AB} - \frac{g'}{2} \Psi_{AB}^2,$$

~YM action, but it is not manifestly real! The first part = SDYM

$$S_{SDYM}[\Psi, \omega] = \int \Psi^{CD} F_{CD}(\omega) = \int \Psi^{CD} H_{CD} \wedge d\omega + \dots$$

$H^{AB} \equiv e^A_{C'} \wedge e^{BC'}$ and $e_{AA'}$ is the vierbein

As different from the flat space perturbation theory, we find an expansion of YM over SDYM, which is quite useful ([Adamo et al](#); [Chicherin et al](#); ...)

Self-dual Theories

- actions are not real in Minkowski space
- actions are simpler than the complete theories
- integrability, instantons (Penrose, Ward, Atiyah, Hitchin, Drinfeld, Manin; ...)
- **SD theories are consistent truncations**, so anything we can compute will be a legitimate observable in the full theory; **any solution of SD is a solution of the full**; ...
- different expansion schemes: instantons instead of flat, MHV, etc.

In general: amplitudes (MHV, BCFW, double-copy, ...), strings, QFT, Twistors, ... encourage to go outside Minkowski

In higher spins: little explored (Adamo, Hähnel, McLoughlin; Krasnov, E.S., Ponomarev, Tran), can be the only reasonably local theories

Twistor-inspired approach

Twistors treat positive and negative helicities differently:

$$\begin{aligned}\nabla_B^{A'} \Psi^{BA(2s-1)} &= 0 && \text{(Penrose, 1965)} \\ \nabla^A_{B'} \Phi^{A(2s-1),B'} &= 0 && \delta\Phi^{A(2s-1),B'} = \nabla^{AB'} \xi^{A(2s-2)}\end{aligned}$$

Known since (Eastwood, Penrose, Wells, 1981), (Hitchin, 1980) almost derived an action

$$S = \int \sqrt{g} \Psi^{BA_2 \dots A_{2s}} \nabla_B^{B'} \Phi_{A_2 \dots A_{2s}, B'}$$

Feature: allow us to put higher spins on any self-dual background, not just flat or (A)dS, c.f. Conformal HS (Adamo, Hähnel, McLoughlin)

N.B: for $s = 1$ we have Ψ^{AB} and $A^{CC'}$, for $s = 2$ Ψ^{ABCD} and $\Phi^{AAA, A'}$

Chiral HiSGRA admits two contractions (Ponomarev) to higher spin extensions of SDYM and SDGR. These HS-SDYM and HS-SDGR can be covariantized (Krasnov, E.S., Tran). We need old/new (Hitchin) free action

$$S = \int \Psi^{A_1 \dots A_{2s}} \wedge H_{A_1 A_2} \wedge \nabla \omega_{A_3 \dots A_{2s-2}}$$

$H^{AB} \equiv e^A_{C'} \wedge e^{BC'}$, where $e_{AA'}$ is the vierbein. Gauge symmetry:

$$\delta \omega^{A(2s-2)} = \nabla \xi^{A(2s-2)} + e^A_{C'} \eta^{A(2s-3), C'}$$

where the algebraic part is to remove the redundant component to have

$$\omega^{A(2s-2)} \ni e_{BB'} \Phi^{A(2s-2)B, B'}$$

For $s = 1$ we have SDYM, for $s = 2$ ω^{AB} is $\frac{1}{2}$ spin-connection and Ψ^{ABCD} is $\frac{1}{2}$ Weyl tensor

Interactions can be introduced by taking sum over s

$$\omega(y) = \sum_k \omega_{A_1 \dots A_k} y^{A_1} \dots y^{A_k}$$

and by replacing $\nabla\omega$ or both H and $\nabla\omega$ with

$$F = d\omega + \frac{1}{2}[\omega, \omega]$$

where the commutator is either due to Yang-Mills groups or due to Poisson bracket on \mathbb{R}^2 of $f(y)$, same as $w_{1+\infty}$:

$$\{f, g\} = \epsilon^{AB} \partial_A f(y) \partial_B g(y)$$

The actions are

$$\text{HS-SDYM : } S = \int \Psi H F \quad \text{HS-SDGR : } S = \int \Psi F F$$

Covariant Chiral Theory in flat/(A)dS

Full covariant form (E.S., Sukhanov, Sharapov, Van Dongen) can be constructed following Vasiliev's commandment:

$$d\Phi = l_2(\Phi, \Phi) + l_3(\Phi, \Phi, \Phi) + \dots$$

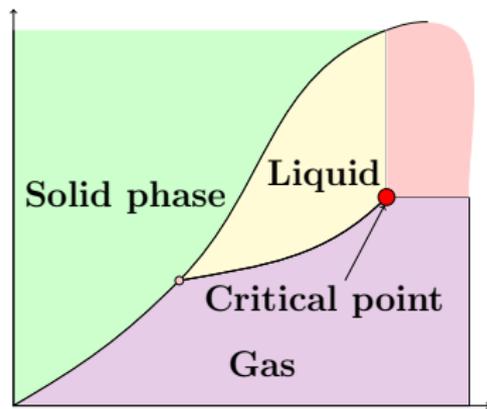
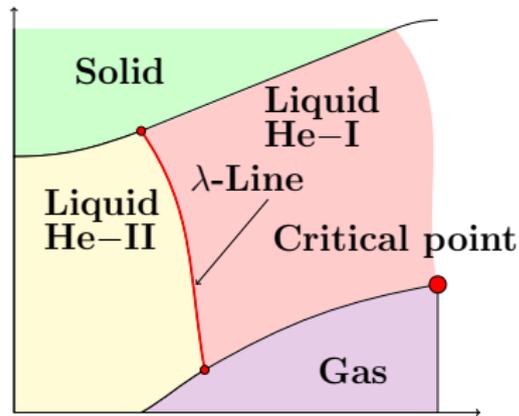
where l_n form L_∞ -algebra; $\Phi = \{\omega, C\}$ and $\omega(y, \bar{y})$, $C(y, \bar{y})$ are generating functions that contain dynamical fields $\omega_{A^{(k)}}$, $\Psi^{A^{(k)}}$ and "derivatives" thereof.

$l_2(\bullet, \bullet) \approx$ higher spin algebra (Weyl algebra): $f(q, p)$, $[q^k, p_j] = i\hbar\delta_j^k$.

Higher maps have something to do with Kontsevich–Shoikhet–Tsygan Formality and must be chosen to respect locality of interactions.

This is the only Lorentz covariant theory with propagating massless higher spin fields. Smooth deformation to (A)dS₄

Chern-Simons Matter Theories and bosonization duality



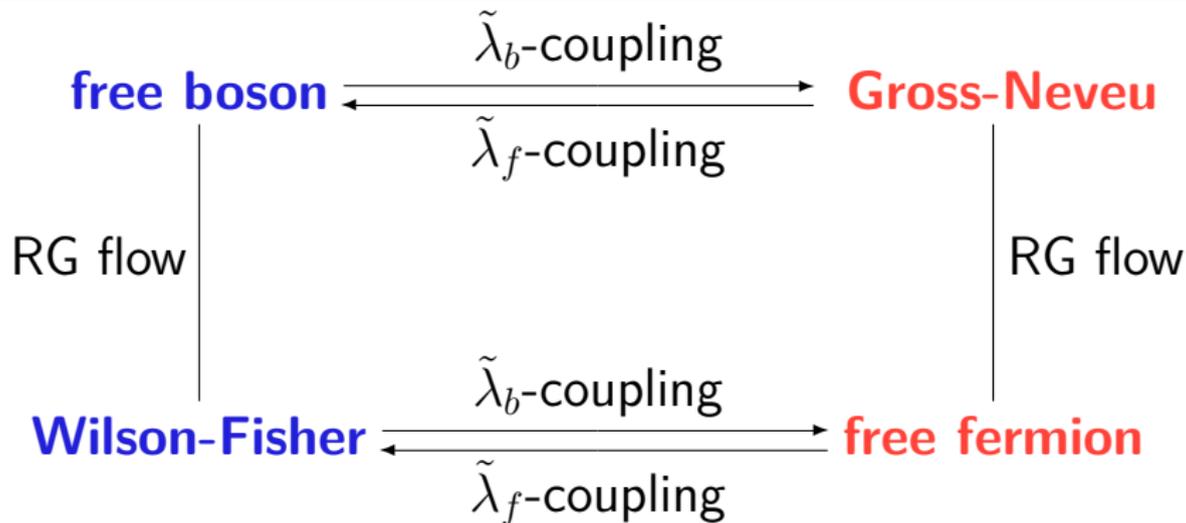
Chern-Simons Matter theories and dualities

In AdS_4/CFT_3 one can do much better — there exists a large class of models, Chern-Simons Matter theories (extends to ABJ(M))

$$\frac{k}{4\pi} S_{CS}(A) + \text{Matter} \begin{cases} (D\phi^i)^2 & \text{free boson} \\ (D\phi^i)^2 + g(\phi^i \phi^i)^2 & \text{Wilson-Fisher (Ising)} \\ \bar{\psi} \not{D} \psi & \text{free fermion} \\ \bar{\psi} \not{D} \psi + g(\bar{\psi} \psi)^2 & \text{Gross-Neveu} \end{cases}$$

- describe physics (Ising, quantum Hall, ...), break parity
- two parameters $\lambda = N/k$, $1/N$ (λ continuous for N large)
- exhibit remarkable dualities, e.g. **3d bosonization duality** (Aharony, Alday, Bissi, Giombi, Karch, Maldacena, Minwalla, Prakash, Seiberg, Tong, Witten, Yacobi, Yin, Zhiboedov, ...)

Chern-Simons Matter theories and dualities



The simplest gauge-invariant operators are higher spin currents

$$J_s = \phi D \dots D \phi$$

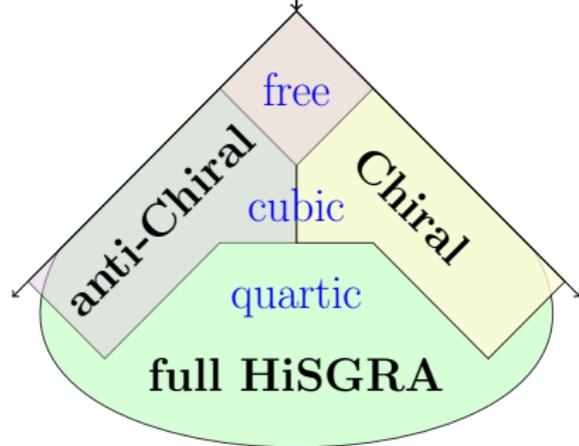
$$J_s = \bar{\psi} \gamma D \dots D \psi$$

which are AdS/CFT dual to higher spin fields

Chiral HiSGRA and Chern-Simons Matter

Chern-Simons Matter Theories

AdS/CFT



(anti)-Chiral Theories are rigid, we need to learn how to glue them

gluing depends on one parameter, which is introduced via simple EM-duality rotation $\Phi_{\pm s} \rightarrow e^{\pm i\theta} \Phi_{\pm s}$

gives all 3-point correlators consistent with (Maldacena, Zhiboedov)

Bosonization is manifest! Concrete predictions from HiSGRA.

(anti)-Chiral Theories provide a complete base for 3-pt amplitudes

$$V_3 = V_{chiral} \oplus \bar{V}_{chiral} \leftrightarrow \langle JJJ \rangle$$

Higher spin symmetry and bosonization duality

Unbroken Higher spin symmetry

In free theories we have ∞ -many conserved $J_s = \phi \partial \dots \partial \phi$ tensors.

Free CFT = Associative (higher spin) algebra

Conserved tensor \rightarrow current \rightarrow symmetry \rightarrow invariants=correlators.

$$\partial \cdot J_s = 0 \quad \implies \quad Q_s = \int J_s \quad \implies \quad [Q, Q] = Q \quad \& \quad [Q, J] = J$$

HS-algebra (free boson) = HS-algebra (free fermion) in $3d$.

Correlators are given by invariants (Sundell, Colombo; Didenko, E.S.; ...)

$$\langle J \dots J \rangle = \text{Tr}(\Psi \star \dots \star \Psi) \quad \Psi \leftrightarrow J$$

where Ψ are coherent states representing J in the higher spin algebra

$$\langle JJJJ \rangle_{F.B.} \sim \cos(Q_{13}^2 + Q_{24}^3 + Q_{31}^4 + Q_{43}^1) \cos(P_{12}) \cos(P_{23}) \cos(P_{34}) \cos(P_{41}) + \dots$$

Slightly-broken Higher spin symmetry is new Virasoro?

In large- N Chern-Simons vector models (e.g. Ising) higher spin symmetry does not disappear completely (Maldacena, Zhiboedov):

$$\partial \cdot J = \frac{1}{N}[JJ] \qquad [Q, J] = J + \frac{1}{N}[JJ]$$

What is the right math? We should deform the algebra together with its action on the module, so that the currents can 'backreact':

$$\delta_\xi J = l_2(\xi, J) + l_3(\xi, J, J) + \dots, \qquad [\delta_{\xi_1}, \delta_{\xi_2}] = \delta_\xi,$$

where $\xi = l_2(\xi_1, \xi_2) + l_3(\xi_1, \xi_2, J) + \dots$. This leads to L_∞ -algebra.

Correlators = invariants of L_∞ -algebra and are unique (Gerasimenko, Sharapov, E.S.), **which proves 3d bosonization duality at least in the large- N** . Without having to compute anything one prediction is

$$\langle J \dots J \rangle = \sum \langle \text{fixed} \rangle_i \times \text{params}$$

Concluding Remarks

- Some HiSGRA do exist, e.g. Chiral HSGRA. It reveals (almost) trivial S -matrix in flat space, but not in AdS
- Chiral HiSGRA is a toy model with stringy features and shows how higher spin fields improve the UV behaviour: **no UV divergences, supersymmetry vs. higher spin symmetry**
- It gives all 3-pt functions in Chern-Simons Matter theories, making new predictions and proves the bosonization duality to this order.
- Higher spin symmetry itself can be useful via L_∞ -algebras. Proof of bosonization duality in the large- N . L_∞ in physics
- **Optimistically: HiSGRA can give viable quantum gravity models not free of direct applications to physics**

Thank you for your attention!